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Revisiting  $\eta'(958)$  nuclear states

$\eta' - {}^{11}\text{C}$  bound states in  ${}^{12}\text{C}(p, d)$  at GSI  
with high-momentum backward protons

R. Sekiya, et al., PRL 136 (2026) 142501

Friedman-Gal, PLB 870 (2025) 139916

Questioning MAMI's extraction

of  $B_{\Lambda}({}_{\Lambda}^3\text{H})$  in  ${}^7\text{Li}(e, e'K^+)$

R. Kino, et al., PRL 136 (2026) 152301

A. Gal, arXiv:2604.18259

# $V_{\text{opt}}(\rho)$ phenomenology background:

$$\Lambda N \Rightarrow V_{\Lambda}^{(2)}(\rho) = -\frac{4\pi}{2\mu_{\Lambda}} b_0^{\text{lab}}(\rho) \rho$$

$$b_0^{\text{lab}}(\rho) = \frac{b_0^{\text{lab}}}{1 + \frac{3k_F}{2\pi} b_0^{\text{lab}}}, \quad b_0^{\text{lab}} = \left(1 + \frac{A-1}{A} \frac{\mu_{\Lambda}}{m_N}\right) b_0,$$

for Pauli correlations, with  $k_F = (3\pi^2 \rho / 2)^{1/3}$ .

Short-range correlations negligible at  $\rho \leq \rho_0$ .

Pauli affects terms beyond  $\rho^{4/3}$ , e.g.,  $\rho^2$ .

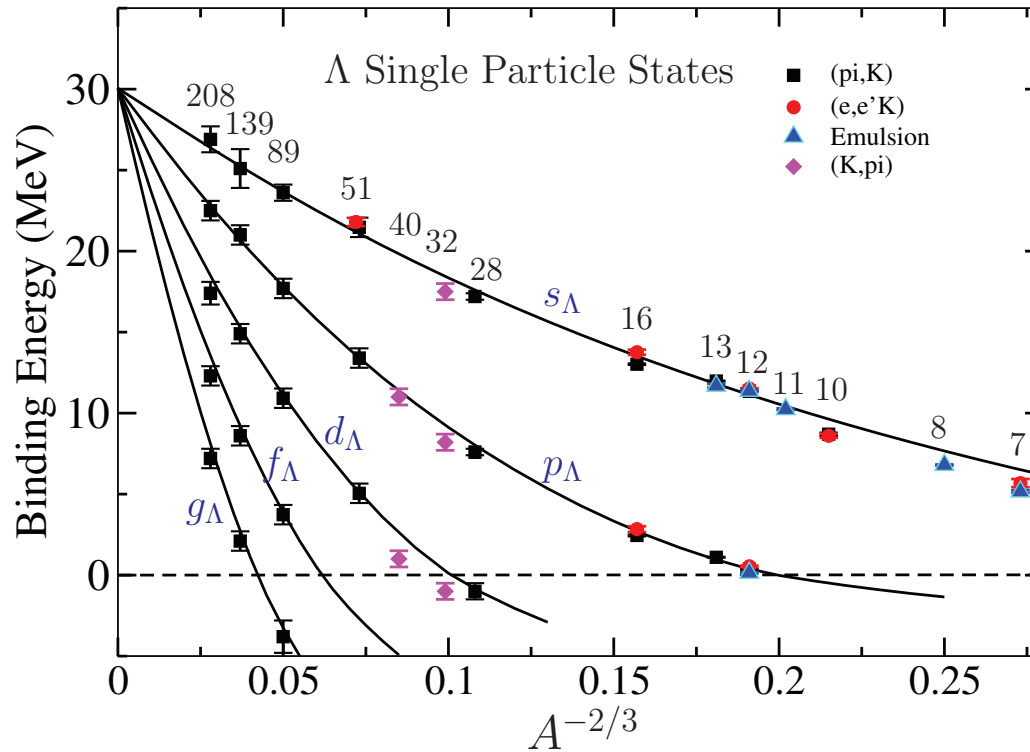
Low density limit:  $b_0 = a_{\Lambda N}$  (scattering length).

Pauli is applied normally only to  $\text{Re } b_0$ .

$$\Lambda NN \Rightarrow V_{\Lambda}^{(3)}(\rho) = +\frac{4\pi}{2\mu_{\Lambda}} \left(1 + \frac{A-2}{A} \frac{\mu_{\Lambda}}{2m_N}\right) B_0 \frac{\rho^2}{\rho_0}.$$

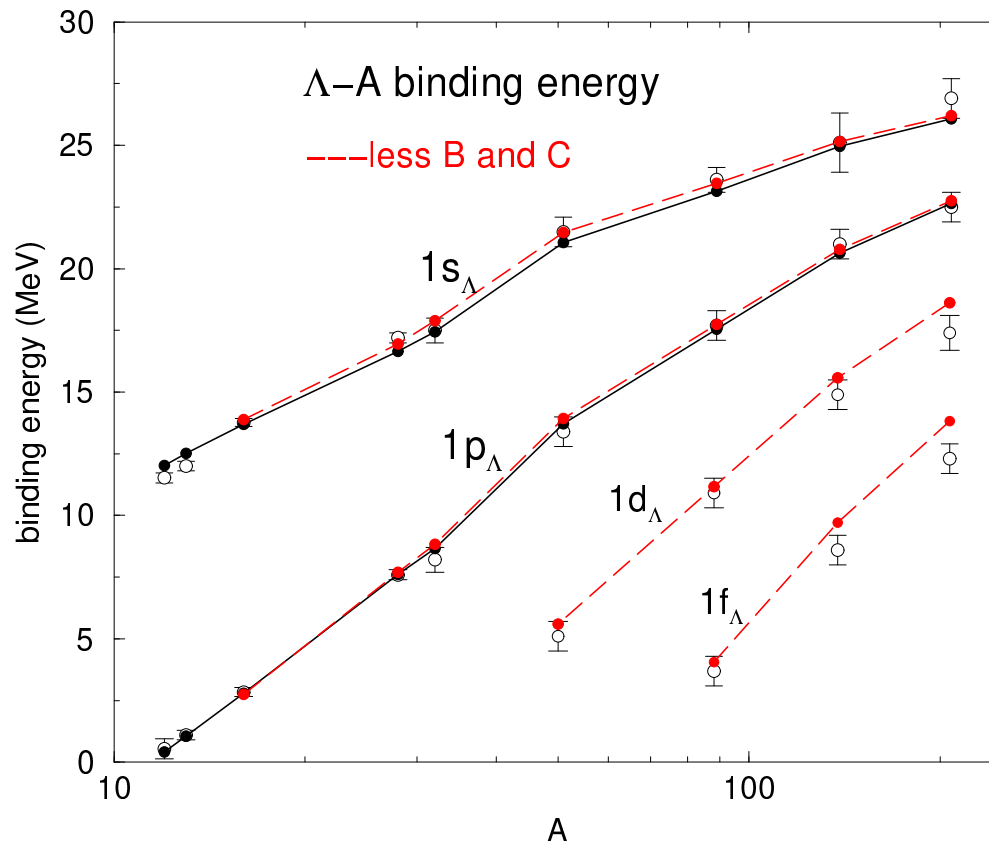
Applying Pauli to  $V_{\Lambda}^{(3)}(\rho)$  has a minor effect.

Update: Millener, Dover, Gal PRC 38, 2700 (1988)



Woods-Saxon  $V = 30.05$  MeV,  $r = 1.165$  fm,  $a = 0.6$  fm

**$B_\Lambda$  values in  ${}^7_\Lambda\text{Li}$  to  ${}^{208}_\Lambda\text{Pb}$  from experiment**  
 and as calculated from a 3-parameter WS potential,  
 suggesting a  $\Lambda$ -nucleus potential depth  **$D_\Lambda \approx -30$  MeV.**  
**Data: Table IV Gal-Hungerford-Millener, RMP 88 (2016) 035004.**



## Fitting $b_0$ & $B_0$ to $B_{\Lambda}(A)$

$\vec{\tau}_1 \cdot \vec{\tau}_2$  in  $\Lambda N_1 N_2$  OPE implies  $\rho^2 \rightarrow (\rho_{\text{sym}}^2 + \rho_{\text{exc}}^2)$ ,  
 resulting in  $\chi^2/19 = 0.95$  for 21 data points.

Friedman-Gal, Acta Phys. Pol. B 57 (2026) 2-A16

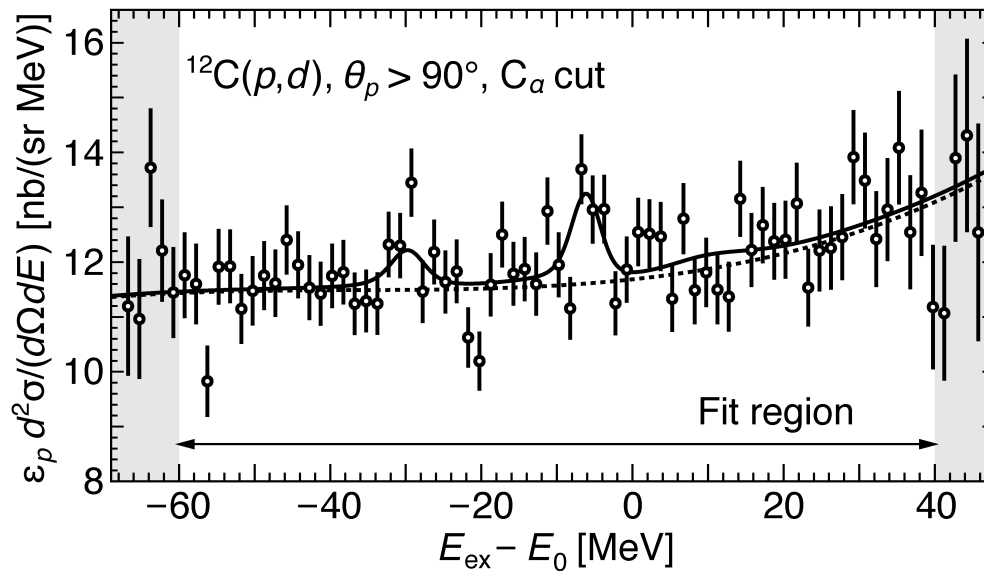
# $\Lambda$ hypernuclei summary

- $V_{\text{opt}}^{\Lambda}(\rho)$  applied to  $(1s_{\Lambda}, 1p_{\Lambda}, 1d_{\Lambda}, 1f_{\Lambda})$  s.p. states across the periodic table.
- Pauli corrected  $\Lambda N$  term, plus  $\Lambda NN$  term.
- Decoupling  $\rho_{\text{exc}}$  from  $\rho_{\text{sym}}$  in  $\Lambda N_1 N_2 \rho^2$  term is motivated by  $\vec{\tau}_1 \cdot \vec{\tau}_2$  isospin structure in  $\Lambda \rightarrow (\Sigma, \Sigma^*) \rightarrow \Lambda$  isovector excitations.
- Depth values  $D_{\Lambda}^{(2)}$  &  $D_{\Lambda}^{(3)}$  fully correlated:  
 $D_{\Lambda}^{(2)} = -37.5 \mp 0.7$  MeV with  $b_0 = 1.32 \pm 0.07$  fm,  
 $D_{\Lambda}^{(3)} = 9.8 \pm 1.2$  MeV,  $D_{\Lambda} = -27.7 \pm 0.5$  MeV.
- $D_{\Lambda}^{(3)} \approx 10$  MeV excludes in EFT  $\Lambda$  hyperons from dense neutron-star matter,  $\mu_{\Lambda} > \mu_n$ , see Gerstung-Kaiser-Weise, EPJA 56 (2020) 175.

# Revisiting $\eta'(958)$ nuclear states

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R. Sekiya, et al., PRL 136 (2026) 142501



Excitation spectrum near  $\eta'$  emission threshold  $E_0$

Bound state signals at  $-30$  and  $-6$  MeV ?

Implying  $V_{\eta'}(\rho_0) \approx -60$  MeV  $\sim V_N(\rho_0) \sim 2 \times V_\Lambda(\rho_0)$

Compatibility with  $a_{\eta'N}$ ?

# $a_{\eta'N}$ experimental input

Near-threshold  $pp \rightarrow pp\eta'$  production @COSY:

$\text{Re } a_{\eta'p} = (0.00 \pm 0.43) \text{ fm}$ ,  $\text{Im } a_{\eta'p} = 0.37_{-0.11}^{+0.02+0.28} \text{ fm}$ .

Near-threshold  $\gamma p \rightarrow \eta'p$  photoproduction experiments:

$|a_{\eta'p}| = (0.403 \pm 0.020 \pm 0.060) \text{ fm} \rightarrow (0.356 \pm 0.012) \text{ fm}$ ,

if no  $\eta'N$  s-wave resonance exists near threshold (1896 MeV).

Using  $V_{\eta'}(\rho)$  from Friedman-Gal, PLB 870 (2025) 139916,

these constraints suggest  $\eta'$  nuclear potential depths

in the range  $D_{\eta'} \approx (-17 \pm 6) - i(27 \pm 6) \text{ MeV}$ ,

with almost no chance for  $\eta' - {}^{11}\text{C}$  bound states.

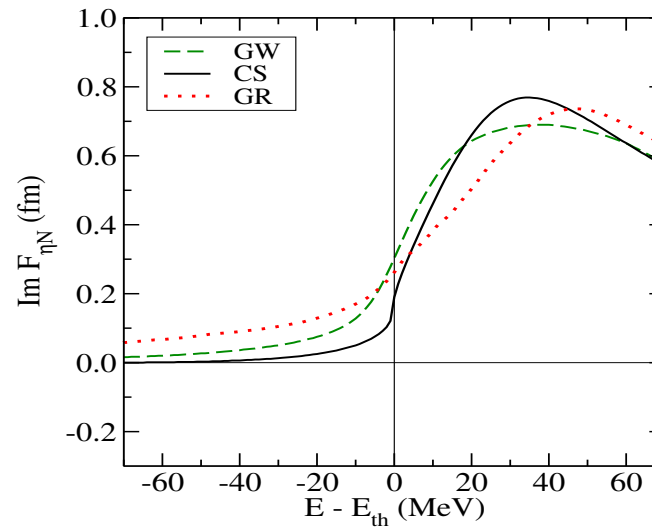
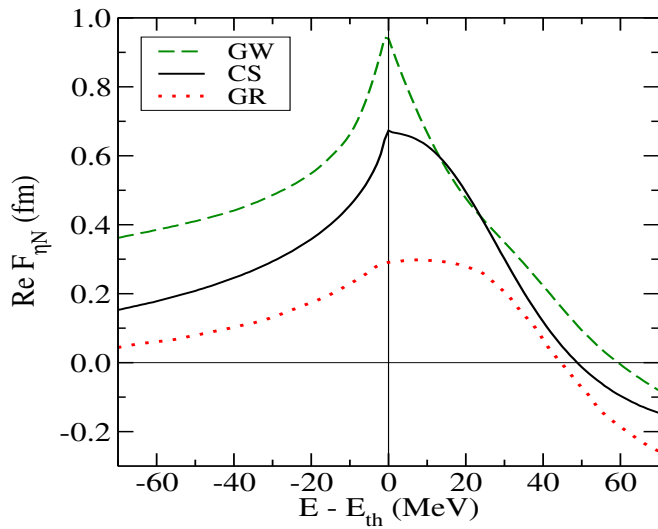
As for the nearby s-wave broad resonance  $N^*(1895)$ ,

look up Bruns-Cieply & Sakai-Jido,

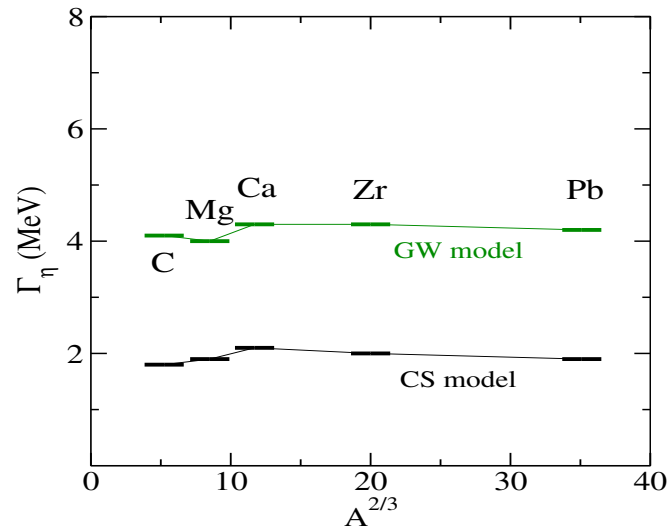
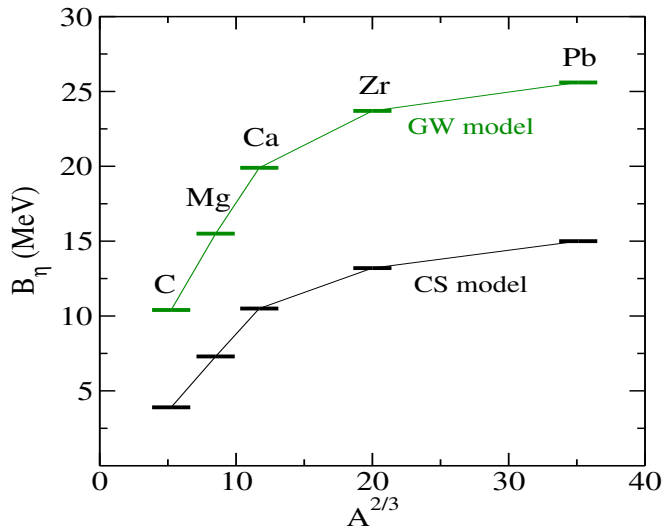
NPA 992 (2019) 121630, PRC 107 (2023) 025207.

Lessons from  $a_{\eta N}$  vs.  $N^*(1535)$  resonance?

# s-wave $F_{\eta N}$ in two $N^*(1535)$ models



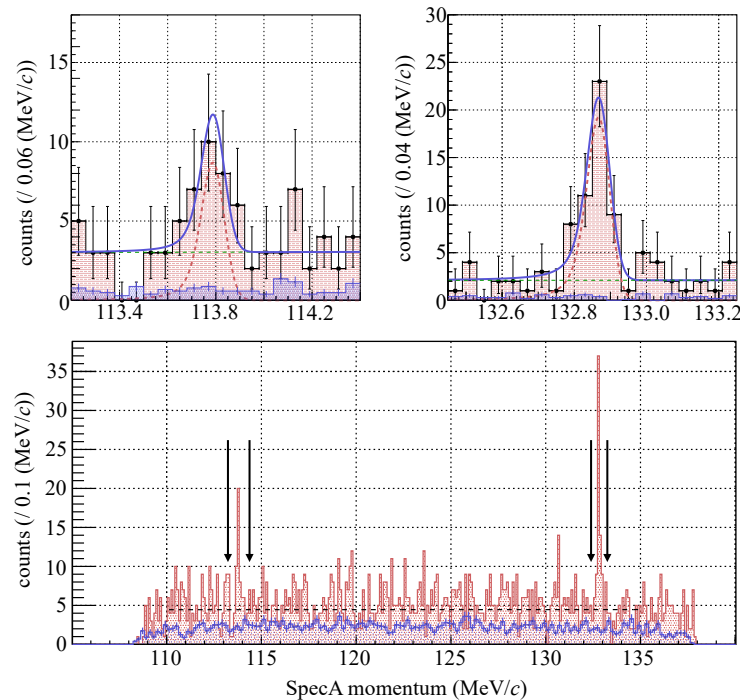
# 1s $\eta$ -nuclear bound states in two models



Cieply-Friedman-Gal-Mareš, NPA 925 (2014) 126

# Questioning MAMI's extraction of $B_{\Lambda}({}^3_{\Lambda}\text{H})$ in ${}^7\text{Li}(e, e'K^+)$

R. Kino, et al., PRL 136 (2026) 152301



Decay  $p(\pi^-)$  spectrum in  ${}^7\text{Li}(e, e'K^+)$  from MAMI  
 $p(\pi^-)$  peaks attributed to  ${}^3_{\Lambda}\text{H}$  (left) and  ${}^4_{\Lambda}\text{H}$  (right).

Why not  ${}^7_{\Lambda}\text{He}$  ?

# How large is $B_{\Lambda}({}^3_{\Lambda}\text{H})$ ?

**MAMI:  $B_{\Lambda}=0.523\pm0.013\pm0.075$  MeV**

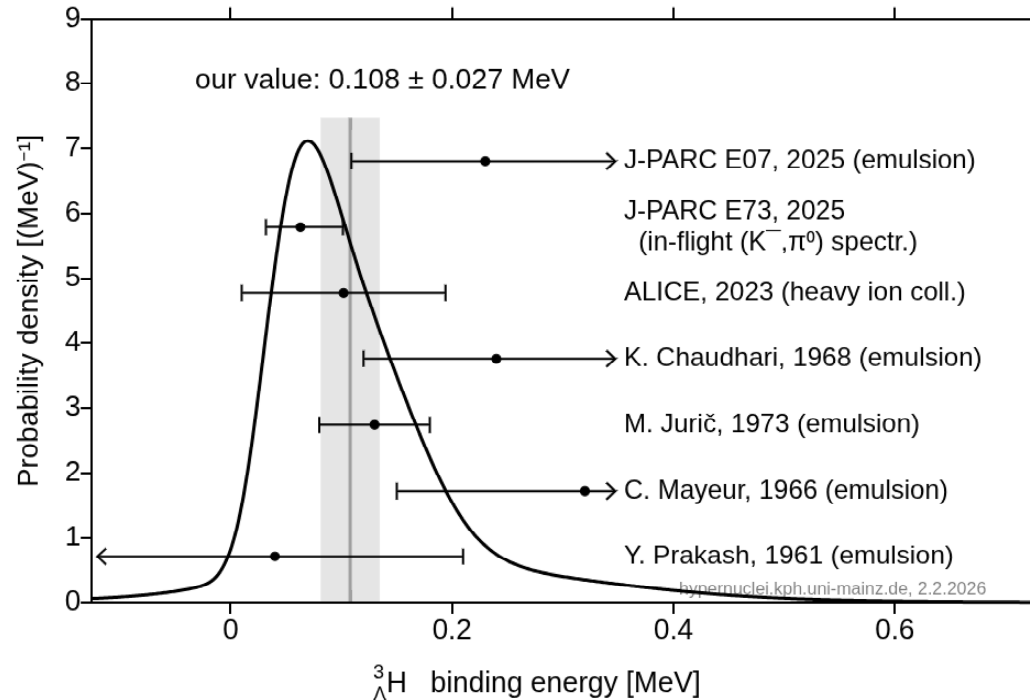
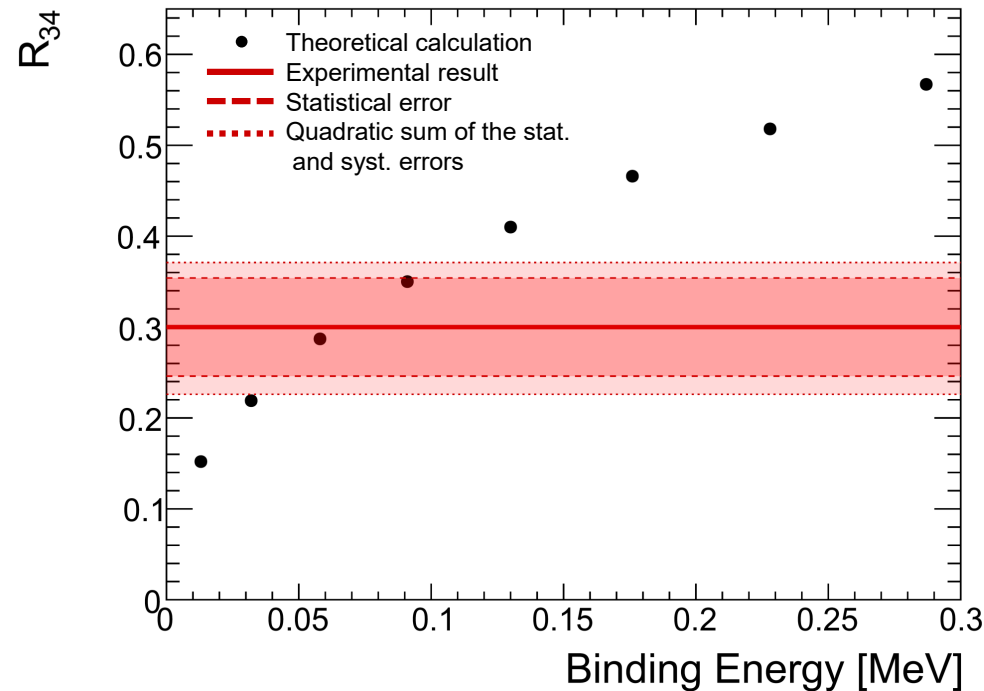


Chart of Hypernuclei **before** MAMI

At present, cites  $0.181^{+0.102}_{-0.040}$  MeV

# J-PARC E73 ${}^3,{}^4\text{He}(K^-, \pi^0)_\Lambda {}^3,{}^4\text{H}$



${}^3,{}^4\text{H}_\Lambda$  production cross section ratio  $R_{34}$

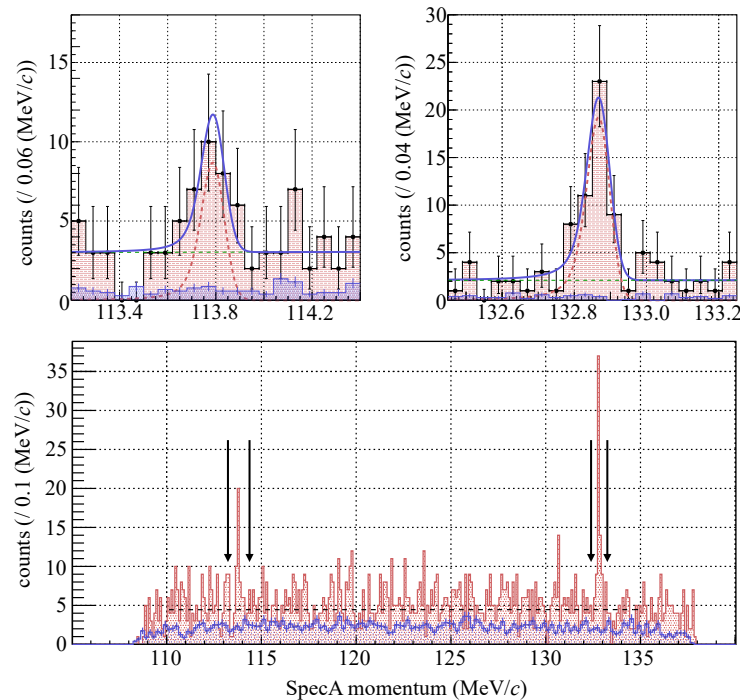
Exp. (red): T. Akaishi, et al., PLB 873 (2026) 140163

Calc. (black): T. Harada, Y. Hirabayashi,  
NPA 1072 (2026) 123417

$$B_\Lambda({}^3\text{H}) = 0.063^{+0.029}_{-0.023}(\text{stat.})^{+0.025}_{-0.021}(\text{syst.})$$

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Why not  ${}^7_{\Lambda}\text{He}$  ?

# Trying out ${}^7_{\Lambda}\text{He}$

A. Gal, arXiv:2604.18259

$p(\pi^-) = 113.8 \text{ MeV}/c$  line reassigned to  
 ${}^7_{\Lambda}\text{He} \rightarrow \pi^- + {}^7\text{Li}^*(0.478 \text{ keV})$ , requiring  
 $B_{\Lambda}({}^7_{\Lambda}\text{He}) = 5.84 \pm 0.07 \text{ MeV}$ ,  $2\sigma$  away from  
JLab's  ${}^7\text{Li}(e, e'K^+)$  value  $5.55 \pm 0.15 \text{ MeV}$ .  
But why decay to  ${}^7\text{Li}(\text{g.s.})$  is not seen?  
Given the  $10^{-10}\text{s}$  weak-decay time scale,  
is  ${}^7\text{Li}^*$  a meaningful final state? It emits  $\gamma$   
much faster than  $\pi^-$  WD, so it is  ${}^7\text{Li}(\text{g.s.})$

that is associated with the  $\pi^-$  WD time scale. Hence, there is only ONE final nuclear state with two amplitudes to reach it. Interference may leave only one of these transitions.

$\eta'$  nuclei conclusion:

add vector mesons to  $N^*(1895)$  models.

$B_\Lambda({}^3_\Lambda\text{H})$ : large (MAMI) or small (E73)?

Note:  $\tau({}^3_\Lambda\text{H}) \approx \tau_\Lambda$  suggests small  $B_\Lambda({}^3_\Lambda\text{H})$ .