



The reaction $\pi N \rightarrow \omega N$ in a dynamical coupled-channel approach (17th International Workshop on Meson Physics)

June 26, 2023 | Yu-Fei Wang | Institute for Advanced Simulation, FZJ

Outline

- 1** Introduction
- 2** Theoretical Framework
- 3** Numerical results
- 4** Conclusion and Outlook

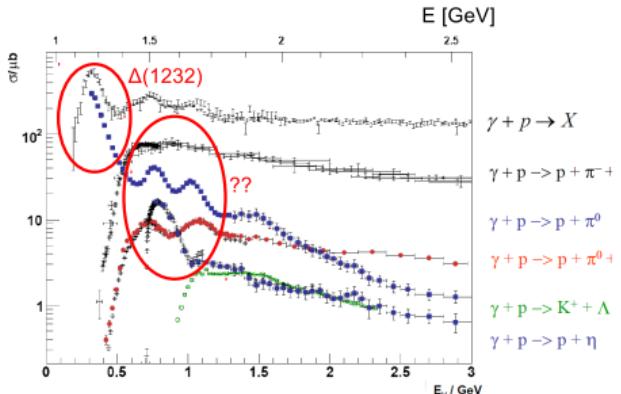
Based on Phys. Rev. D **106** 094031 (2022)

In collaboration with D. Rönchen, U.-G. Meißner, Y. Lu, C.-W. Shen, and J.-J. Wu

Introduction

Hadron spectroscopy

- Hadron spectroscopy → crucial for understanding QCD
- Low energy region → effective theories. High energy region → asymptotic freedom.
- Intermediate energy region → **abundant experimental observations**, involved coupled-channel dynamics
- Textbook Breit-Wigner (BW) description sometimes fails
 - resonance v.s. background
 - interference



[source: ELSA; data: ELSA, JLab, MAMI]

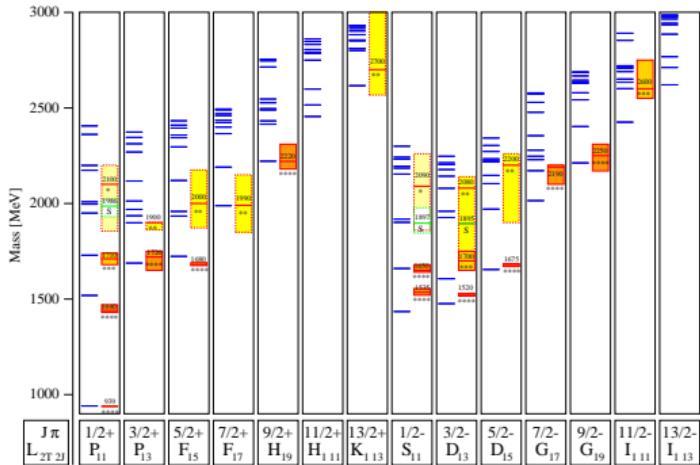
Introduction

Hadron spectroscopy

- Extraction of resonances → partial wave analyses (PWA)
- Decomposition under JLS basis

$$T \rightarrow T^{JLS}$$

- Various methods
 - Unitary isobar models → unitary amplitudes + BW
[MAID, Yerevan/JLab, KSU, ...]
 - K-matrix Unitarization → on-shell intermediate states
[GWU/SAID, BrGa, Gießen, ...]
 - Dynamical coupled-channel (DCC) approaches → interaction potentials + scattering equations (off-shell intermediate states)
[ANL-Osaka (EBAC), Dubna-Mainz-Taipeh, ...] & Jülich-Bonn Model
- ...



[spectra: PDG 2000. quark model calculations: Löring et. al., EPJA 10, 395 (2001)]

Introduction

Jülich-Bonn Model

Jülich-Bonn Model

- Powerful tool for the PWA
- Parameters → fit to a worldwide collection of data
- Unitarity, analyticity → searching resonance poles on the second sheet [Döring et. al., NPA 829, 170 (2009)]
- Applications
 - Hadronic part: πN induced reactions [Schütz et. al., PRC 51, 1374 (1995)] [Schütz et. al., PRC 49, 2671 (1994)][Schütz et. al., PRC 57, 1464 (1998)] [Krehl et. al., PRC 62, 025207 (2000)][Gasparyan et. al., PRC 68, 045207 (2003)][Döring et. al., NPA 851, 58 (2011)] [Rönchen et. al., EPJA 49, 44 (2013)][Wang et. al., PRD 106, 094031 (2022)]
 - Photoproduction [Rönchen et. al., EPJA 50, 101 (2014)] [Rönchen et. al., EPJA 51, 70 (2015)][Rönchen et. al., EPJA 54, 110 (2018)] [Rönchen et. al., EPJA 558, 229 (2022)]
 - Electroproduction (Jülich-Bonn-Washington) [Mai et. al., PRC 103, 065204 (2021)] [Mai et. al., PRC 106, 015201 (2022)]
 - Hidden charm sector and P_c states [Shen et. al., CPC 42, 023106 (2018)] [Wang et. al., EPJC 82, 497 (2022)]

ωN physics

- Low-density nuclear matter → QCD chiral symmetry
- Vector meson dominance [Gell-Mann & Zachariasen, PR 124, 953 (1961)] → ω in the nuclear matter
- ω plays a very important role in the EOS of the neutron stars [H. Shen et. al., NPA 637, 435 (1998)]
- The ωN elastic scattering length → in-medium bound states??

Cannot be measured directly by experiments!! → comprehensive models like Jülich-Bonn

Theoretical Framework

Dynamics I

Central part of this model: hadronic (πN induced) reactions

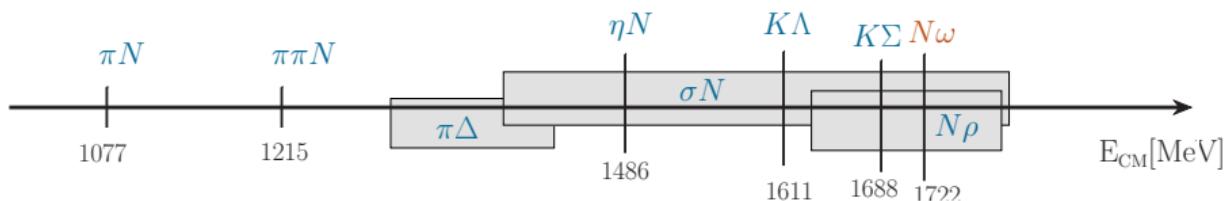
The Lippmann-Schwinger-like equation (CM frame)

$$T_{\mu\nu}(p'', p', z) = V_{\mu\nu}(p'', p', z) + \sum_{\kappa} \int_0^{\infty} p^2 dp V_{\mu\kappa}(p'', p, z) G_{\kappa}(p, z) T_{\kappa\nu}(p, p', z)$$

- Reaction channels $\nu \rightarrow \kappa \rightarrow \mu$ (after PW and isospin projection, JLS basis [Jacob & Wick, Annals Phys. 7, 404 (1959)], $J \leq 9/2$)
- Propagator: G ($\pi\pi N$ channel: effective channels $\rho N, \sigma N, \pi\Delta$. $E/\omega/z$ - baryon/meson/total energy.)

$$G_{\kappa}(z, p) = \begin{cases} (z - E_{\kappa} - \omega_{\kappa} + i0^{+})^{-1} & \text{(if } \kappa \text{ is a two-body channel)} \\ [z - E_{\kappa} - \omega_{\kappa} - \Sigma_{\kappa}(z, p) + i0^{+}]^{-1} & \text{(if } \kappa \text{ is an effective channel).} \end{cases}$$

- Observables \rightarrow dimensionless amplitude $\tau_{\mu\nu} = -\pi\sqrt{\rho_{\mu}\rho_{\nu}}T_{\mu\nu}$, ρ : kinematic factor
- Second Riemann sheet \rightarrow analytical continuation of G [Döring et. al., NPA 829, 170 (2009)]



Theoretical Framework

Dynamics II

■ Separating the amplitude

→ with/without s -channel poles $T = T^P + T^{NP}$

$$T^{NP} = V^{NP} + \sum \int p^2 dp V^{NP} G T^{NP}$$

$$T_{\mu\nu}^P(p'', p', z) = \sum_{i,j} \Gamma_{\mu,i}^a(p'') D_{ij}(z) \Gamma_{\nu,j}^c(p'), \\ (D^{-1})_{ij} = \delta_{ij}(z - m_i^b) - \Sigma_{ij}(z)$$

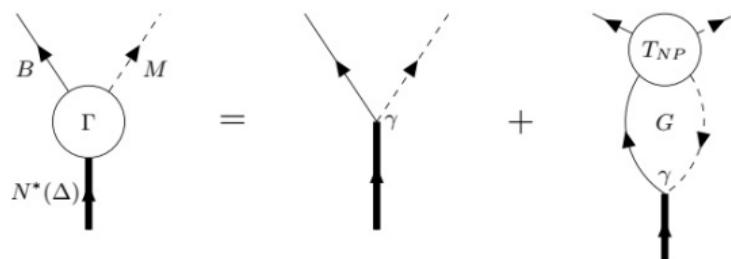
- $\Gamma(\gamma)$: the dressed (bare) vertices
(a - annihilation, c - creation)
- Σ : self-energy functions
- Nucleon mass renormalization

■ $V^{NP}, \gamma \rightarrow$ constructed from effective Lagrangians
+ regulators (cut-offs)
(details: Supplemental material

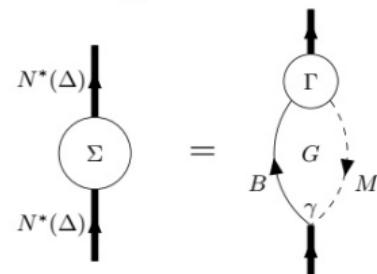
[Wang et. al., PRD 106, 094031 (2022)]

■ s -channel contact terms: $D \sim (1 - \Sigma)^{-1}$

[Rönchen et. al., EPJA 51, 70 (2015)]



(a) The vertex.



(b) The self energy.

Numerical results

Numerical details

- Database → over 9000 points, 174 of $\pi N \rightarrow \omega N$
Energy $\in [1078, 2300]$ MeV
- Parameters: s -channel bare couplings + cut-offs
(V^{NP})
 $\rightarrow 225 + 79$
- Haftl-Tabakin matrix inversion
→ discretization via the Gaussian points

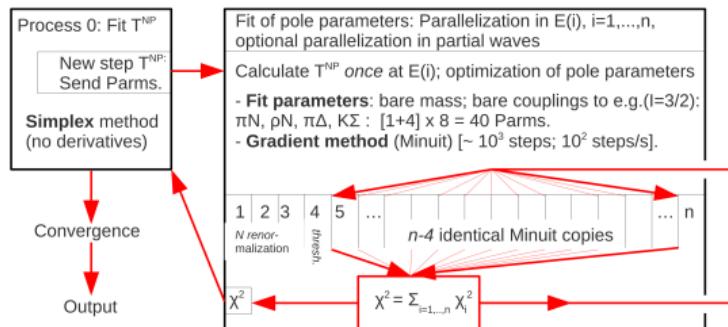
[Haftel & Tabakin, NPA 158, 1 (1970)]

$$T_{ab}^{NP} = V_{ab}^{NP} + \sum_{i=1}^n p_i^2 w_i V_{ai}^{NP} G_i T_{ib}^{NP}, \quad \hat{T} = (1 - \hat{V} \hat{G})^{-1} \hat{V}$$

- Supercomputer JURECA

[JSC, Journal of large-scale research facilities 7 (2021)]

- NP parameters are much slower → nested fitting



Numerical fit

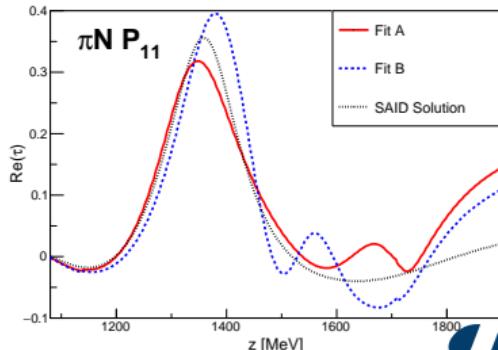
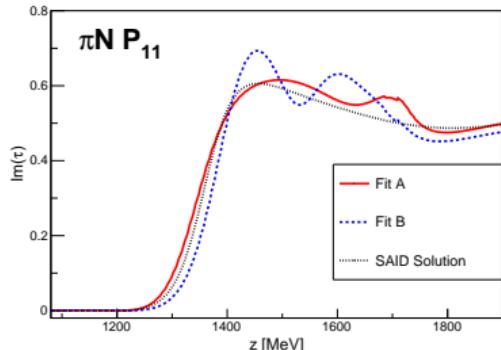
Estimation of the errors

■ The statistics

- Energy-dependent solutions of πN amplitudes [Arndt et. al., PRC 74, 045205 (2006)] → no errors
- Some problematic data points of ηN [Brown et. al., NPB 153, 89 (1979)]
- Extra weights on important data sets (e.g. ωN)
- Impossible to switch on all parameters in one attempt
- Estimation of the uncertainties → fits with different initial values

■ Two fits → equally good fit qualities

- Fit A → from intermediate values of [Röchen et. al., EPJA 54, 110 (2018)]
- Fit B → an extra narrow resonance in P_{11} wave ($J^P = \frac{1}{2}^+$, $z_r = 1585 - 35i$ MeV)



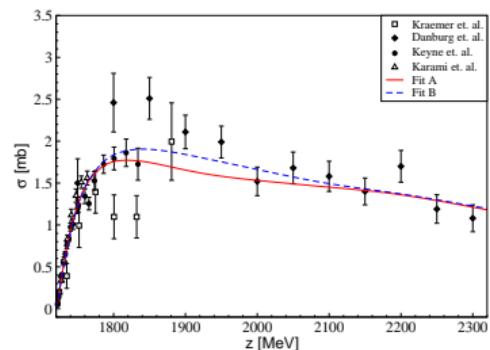
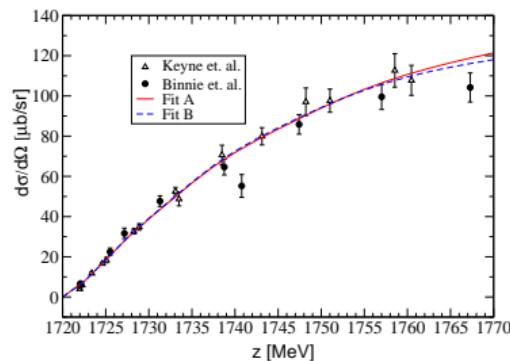
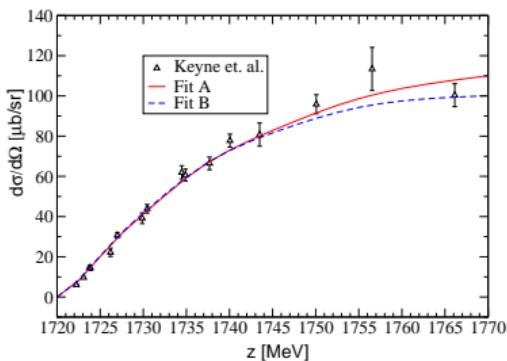
Numerical fit

Fit Results

ωN Data: [Danburg et. al., PRD 2, 2564 (1970)] [Kraemer et. al., PR 136, B496 (1964)] [Binnie et. al., PRD 8, 2789 (1973)] [Keyne et. al., PRD 14, 28 (1976)] [Karami et. al., NPB 154, 503 (1979)]

Other channels: see the [website](#)

First: backward differential cross section. Second: forward. Third: total cross section.

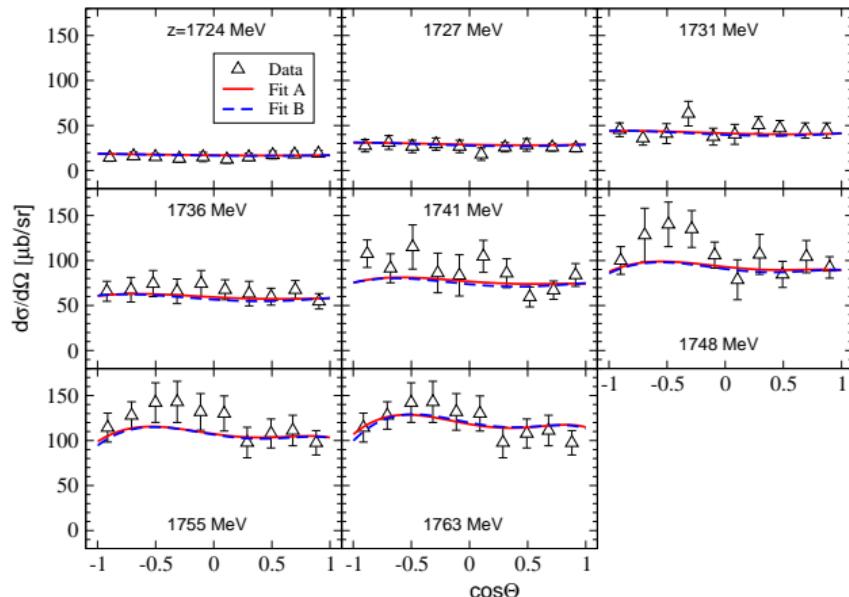


Numerical fit

Fit Results

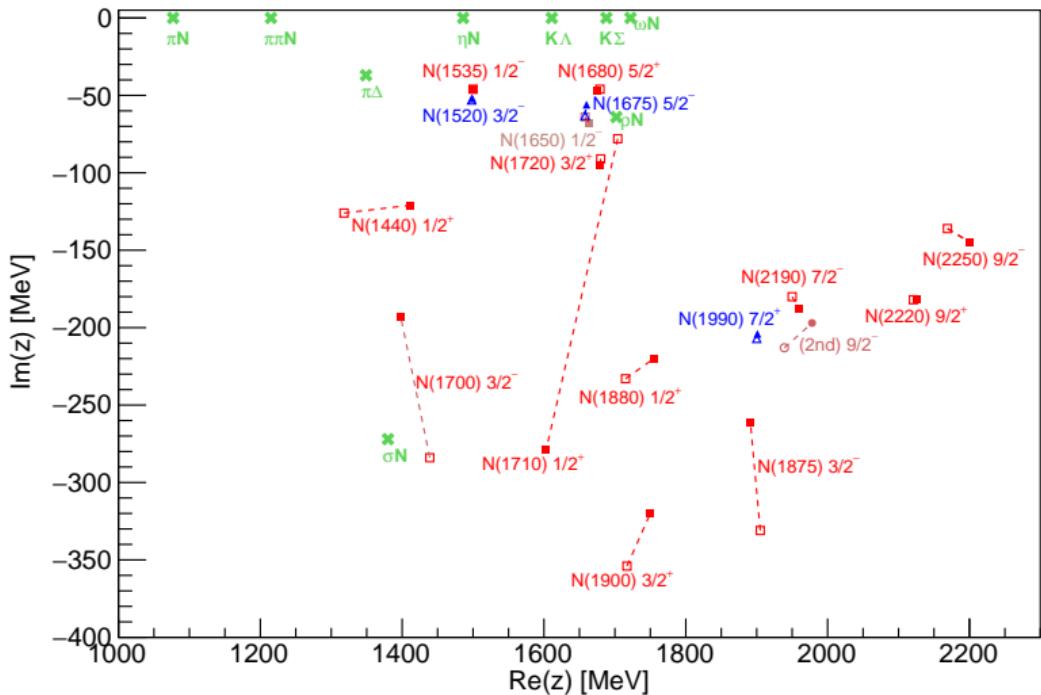
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Other channels: see the [website](#)



Selected Results

N^* Spectra (J^P convention. Empty symbols: fit A. Filled: fit B.)



Selected Results

N^* Couplings

Physical couplings → normalized residues at $z_r = M_r - \frac{i}{2} \Gamma_r$ [PDG] $\tau_{\mu\nu}^{II} \sim \frac{R_\mu R_\nu}{z_r - z} + \dots$, $NR_\mu \equiv \frac{2R_{\pi N}}{\Gamma_r} \times R_\mu$

Our results

- ωN mainly couples to lower states ($|NR| > 0.5$): $N(1535) \frac{1}{2}^-$, $N(1710) \frac{1}{2}^+$ and $N(1680) \frac{5}{2}^+$
- Very large bare couplings → $N^*(1535)$ and $N^*(1710)$
- Fit C (constraining the bare couplings) failed → left for the future with photonproduction included
- Higher states → $N(2250) \frac{9}{2}^-$ relatively important ($Br > 10\%$)

In the literature: which states are important for ωN

- $N(1720) \frac{3}{2}^+$ and $N(1680) \frac{5}{2}^+$ [Zhao, PRC 63, 025203 (2001)]
- $N(1535) \frac{1}{2}^-$, $N(1650) \frac{1}{2}^-$ and $N(1520) \frac{3}{2}^-$ [Lutz et. al., NPA 706, 431 (2002)]
- $N(1710) \frac{1}{2}^+$, $N(1675) \frac{5}{2}^-$ and $N(1680) \frac{5}{2}^+$ [Penner & Mosel, PRC 66, 055211 (2002)][Penner & Mosel, PRC 66, 055212 (2002)][Shklyar et. al., PRC 71, 055206 (2005)]
- $N(1675) \frac{5}{2}^-$ and $N(1680) \frac{5}{2}^+ \rightarrow$ very large bare couplings [Muehlich et. al., NPA 780, 187 (2006)]

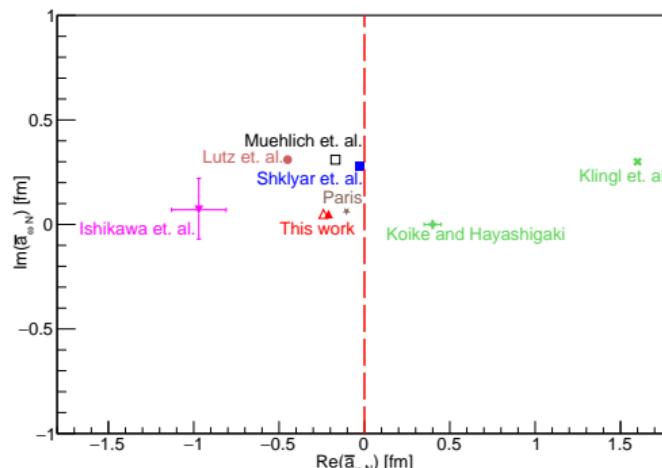
Selected Results

ωN Scattering Length

- Definition $\rightarrow a_\kappa \equiv \lim_{p_\kappa \rightarrow 0} p_\kappa^{-1} \tan \tilde{\delta}_\kappa^{(L=0)} = \lim_{p_\kappa \rightarrow 0} p_\kappa^{-1} \tau_{\kappa\kappa}^{(L=0)}$ ($\tilde{\delta}$: generalized phase shift)
- Spin average of ωN $\rightarrow \bar{a}_{\omega N} = \frac{1}{3}a_{\omega N}(S=\frac{1}{2}) + \frac{2}{3}a_{\omega N}(S=\frac{3}{2})$
- Fit A: $\bar{a}_{\omega N} = (-0.24 + 0.05i)$ fm. Fit B: $\bar{a}_{\omega N} = (-0.21 + 0.05i)$ fm.
- $\text{Re}\bar{a} < 0 \rightarrow$ in-medium bound states tend not to be formed

Other results: [Koike & Hayashigaki, PTP 98, 631 (1997)][Klingl et. al., NPA 650, 299 (1999)][Lutz et. al., NPA 706, 431 (2002)][Shklyar et. al., PRC 71, 055206 (2005)]

[Muehlich et. al., NPA 780, 187 (2006)][Paris, PRC 79, 025208 (2009)][Ishikawa et. al., PRC 101, 052201 (2020)]



Conclusion and Outlook

Conclusion

- The Jülich-Bonn Model: a powerful model for the partial-wave analyses and extraction of the hadron spectra
- Study of the ωN channel
 - More than 9000 data points in πN induced reactions are refitted.
 - There are two fit solutions to evaluate the uncertainties.
 - Hadron spectra are reanalysed.
 - ωN couples mainly to lower states: $N(1535) \frac{1}{2}^-$, $N(1710) \frac{1}{2}^+$ and $N(1680) \frac{5}{2}^+$.
 - Negative real part of the scattering length of ωN .

Outlook

- ω photonproduction → abundant and precise experimental measurements
- Numerical fit of the hidden charm sector
- Study of $\bar{K}N$ induced reactions
- More statistics → πN correlation matrix [Döring et. al., PRC 93, 065205 (2016)]
- LASSO method [Tibshirani, Statistics in medicine 16, 385 (1997)]
- The ω meson in the nuclear matter

*Thank
you*

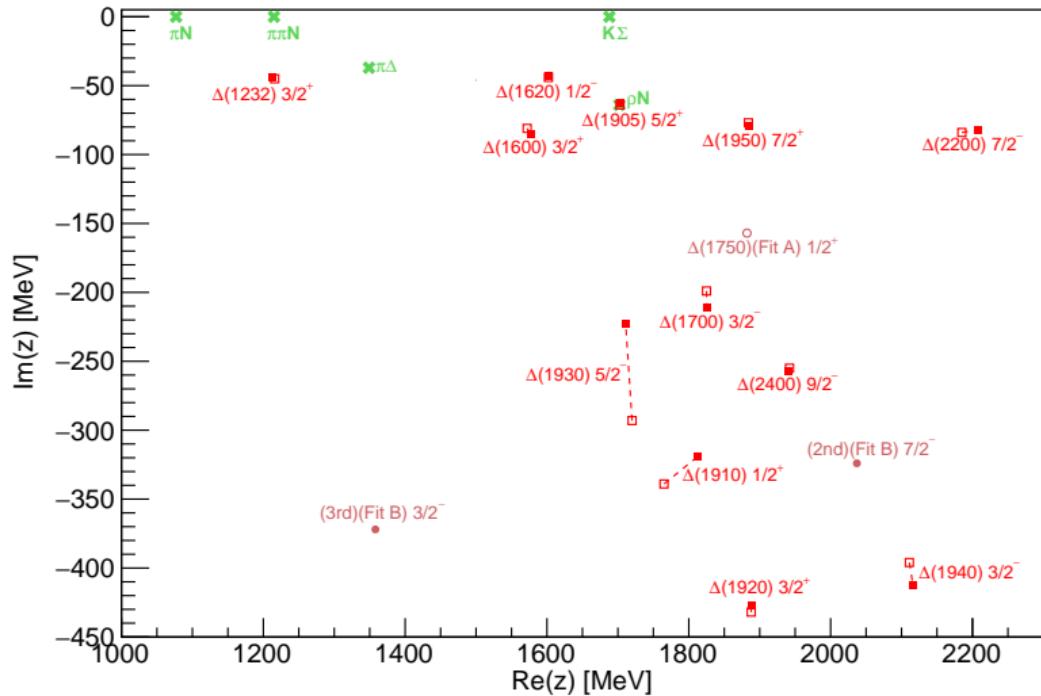


Backups

Feynman diagrams

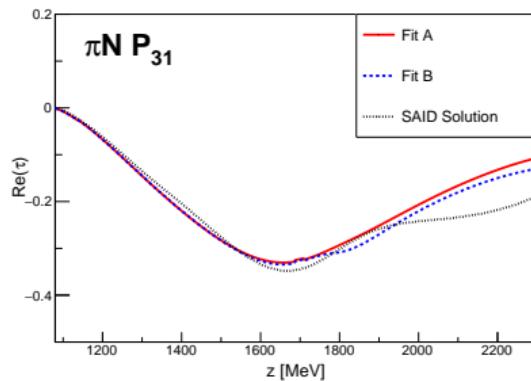
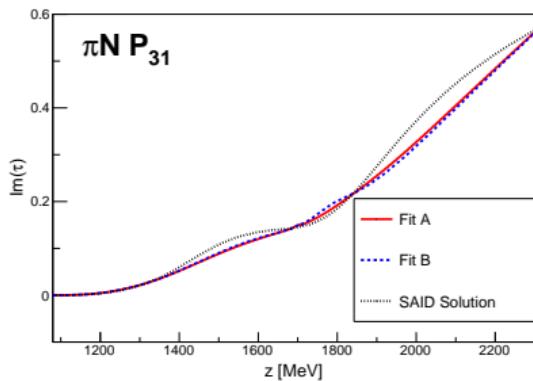
πN	$\pi \Delta$	σN	ηN	$K\Lambda$	$K\Sigma$	ρN	ωN
πN	$\rho\sigma$	ρ	π	a_0	K^*	K^*	$\pi\omega a_1$
$\pi \Delta$	—	ρ	π				π
σN	—	—	σ				
ηN	—	—	—	f_0	K^*	K^*	ω
$K\Lambda$	—	—	—	—	$f_0\omega$	ρa_0	KK^*
$K\Sigma$	—	—	—	—	—	$f_0\omega\rho a_0$	KK^*
ρN	—	—	—	—	—	—	ρ
ωN	—	—	—	—	—	—	σ

Δ spectra



Δ spectra

- Influence of $\omega N \rightarrow$ rearrangement of $I = 1/2, 3/2$ contributions via $K^0\Sigma^0$ and $K^+\Sigma^-$
- Channels of isospin $I = 3/2 \rightarrow$ smaller database
- The $\Delta(1910) \frac{1}{2}^+$ (P_{31} wave of πN) \rightarrow much broader $1765 - 339i(1813 - 319i)$ MeV while the line-shape is well described



Pole positions

Resonances	Fit A	Fit B	Estimation of PDG
N(1535) $\frac{1}{2}^-$	1500 – 46 <i>i</i>	1499 – 46 <i>i</i>	1510 – 65 <i>i</i> (*****)
N(1650) $\frac{1}{2}^-$	1658 – 64 <i>i</i>	1664 – 68 <i>i</i>	1655 – 68 <i>i</i> (*****)
N(1440) $\frac{1}{2}^+$ (NP)	1318 – 126 <i>i</i>	1411 – 121 <i>i</i>	1370 – 88 <i>i</i> (*****)
N(1710) $\frac{1}{2}^+$	1704 – 78 <i>i</i>	1603 – 279 <i>i</i>	1700 – 60 <i>i</i> (*****)
N(1880) $\frac{1}{2}^+$ (NP)	1715 – 233 <i>i</i>	1755 – 220 <i>i</i>	1860 – 115 <i>i</i> (****)
N(1720) $\frac{3}{2}^+$	1680 – 91 <i>i</i>	1679 – 95 <i>i</i>	1675 – 125 <i>i</i> (*****)
N(1900) $\frac{3}{2}^+$	1717 – 354 <i>i</i>	1750 – 320 <i>i</i>	1920 – 75 <i>i</i> (*****)
N(1520) $\frac{3}{2}^-$	1498 – 53 <i>i</i>	1499 – 52 <i>i</i>	1510 – 55 <i>i</i> (*****)
N(1700) $\frac{3}{2}^-$ (NP)	1439 – 284 <i>i</i>	1398 – 193 <i>i</i>	1700 – 100 <i>i</i> (****)
N(1875) $\frac{3}{2}^-$ (NP)	1905 – 331 <i>i</i>	1891 – 261 <i>i</i>	1900 – 80 <i>i</i> (***)
N(1675) $\frac{5}{2}^-$	1658 – 63 <i>i</i>	1660 – 56 <i>i</i>	1660 – 68 <i>i</i> (*****)
N(1680) $\frac{5}{2}^+$	1679 – 46 <i>i</i>	1674 – 47 <i>i</i>	1675 – 60 <i>i</i> (*****)
N(1990) $\frac{7}{2}^+$	1900 – 207 <i>i</i>	1901 – 204 <i>i</i>	omitted (**)
N(2190) $\frac{7}{2}^-$	1950 – 180 <i>i</i>	1960 – 188 <i>i</i>	2100 – 200 <i>i</i> (*****)
N(2250) $\frac{9}{2}^-$	2169 – 136 <i>i</i>	2201 – 145 <i>i</i>	2200 – 210 <i>i</i> (*****)
2nd pole $\frac{9}{2}^-$ (NP)	1939 – 213 <i>i</i>	1978 – 197 <i>i</i>	—
N(2220) $\frac{9}{2}^+$	2121 – 182 <i>i</i>	2125 – 182 <i>i</i>	2170 – 200 <i>i</i> (*****)

Pole positions

Resonances	Fit A	Fit B	Estimation of PDG
$\Delta(1620) \frac{1}{2}^-$	$1602 - 44i$	$1602 - 43i$	$1600 - 60i$ (*****)
$\Delta(1750) \frac{1}{2}^+ (\text{NP})$	$1882 - 157i$	—	omitted (*)
$\Delta(1910) \frac{1}{2}^+$	$1765 - 339i$	$1813 - 319i$	$1860 - 150i$ (*****)
$\Delta(1232) \frac{3}{2}^+$	$1216 - 45i$	$1213 - 44i$	$1210 - 50i$ (*****)
$\Delta(1600) \frac{3}{2}^+ (\text{NP})$	$1572 - 81i$	$1577 - 85i$	$1510 - 135i$ (*****)
$\Delta(1920) \frac{3}{2}^+$	$1888 - 432i$	$1888 - 427i$	$1900 - 150i$ (***)
$\Delta(1700) \frac{3}{2}^-$	$1825 - 199i$	$1825 - 211i$	$1665 - 125i$ (*****)
$\Delta(1940) \frac{3}{2}^- (\text{NP})$	$2111 - 396i$	$2116 - 412i$	$1950 - 175i$ (**)
3rd pole $\frac{3}{2}^- (\text{NP})$	—	$1358 - 372i$	—
$\Delta(1930) \frac{5}{2}^-$	$1720 - 293i$	$1711 - 223i$	$1880 - 140i$ (***)
$\Delta(1905) \frac{5}{2}^+$	$1703 - 64i$	$1703 - 63i$	$1800 - 150i$ (*****)
$\Delta(1950) \frac{7}{2}^+$	$1884 - 77i$	$1885 - 79i$	$1880 - 120i$ (*****)
$\Delta(2200) \frac{7}{2}^-$	$2185 - 84i$	$2208 - 82i$	$2100 - 170i$ (***)
2nd pole $\frac{7}{2}^- (\text{NP})$	—	$2037 - 324i$	—
$\Delta(2400) \frac{9}{2}^-$	$1942 - 255i$	$1941 - 257i$	omitted (**)

Normalized residues: ωN channel

TABLE V. The normalized residues of the N^* states for the ωN channel. The values are written in the form (NR, θ) , with the phase θ in units of degrees. In each cell, the first (second) value is from fit A (B). The three sub-channels are (1) $|J - L| = \frac{1}{2}$, $S = \frac{1}{2}$; (2) $|J - L| = \frac{1}{2}$, $S = \frac{3}{2}$; (3) $|J - L| = \frac{3}{2}$, $S = \frac{3}{2}$.

Resonances	Channel (1)	Channel (2)	Channel (3)
$N(1535)\frac{1}{2}^-$	$(1.13, -156^\circ)$ $(1.13, -163^\circ)$	0	$(0.14, 26^\circ)$ $(0.13, 18^\circ)$
$N(1650)\frac{1}{2}^-$	$(0.19, 156^\circ)$ $(0.14, 148^\circ)$	0	$(0.02, -9^\circ)$ $(0.02, -10^\circ)$
$N(1440)\frac{1}{2}^+$	$(0.18, -37^\circ)$ $(0.21, 23^\circ)$	$(0.34, 1^\circ)$ $(0.42, 64^\circ)$	0
$N(1710)\frac{1}{2}^+$	$(0.10, 158^\circ)$ $(0.27, -86^\circ)$	$(0.56, -172^\circ)$ $(0.73, -59^\circ)$	0
$N(1880)\frac{1}{2}^+$	$(0.01, -24^\circ)$ $(0.00, 152^\circ)$	$(0.03, 31^\circ)$ $(0.02, 157^\circ)$	0
$N(1720)\frac{3}{2}^+$	$(0.01, 150^\circ)$ $(0.01, 155^\circ)$	$(0.05, -178^\circ)$ $(0.06, -178^\circ)$	$(0.00, 69^\circ)$ $(0.00, 56^\circ)$
$N(1900)\frac{3}{2}^+$	$(0.00, 33^\circ)$ $(0.01, -19^\circ)$	$(0.02, 138^\circ)$ $(0.01, 91^\circ)$	$(0.00, 6^\circ)$ $(0.00, -75^\circ)$
$N(1520)\frac{3}{2}^-$	$(0.09, 139^\circ)$ $(0.14, 141^\circ)$	$(0.04, 102^\circ)$ $(0.07, 115^\circ)$	$(0.16, -108^\circ)$ $(0.22, -99^\circ)$
$N(1700)\frac{3}{2}^-$	$(0.02, -35^\circ)$ $(0.03, 20^\circ)$	$(0.01, -123^\circ)$ $(0.01, 5^\circ)$	$(0.02, -4^\circ)$ $(0.01, 87^\circ)$
$N(1875)\frac{3}{2}^-$	$(0.00, -110^\circ)$ $(0.00, -82^\circ)$	$(0.00, -172^\circ)$ $(0.00, -114^\circ)$	$(0.00, -157^\circ)$ $(0.00, -105^\circ)$
$N(1675)\frac{5}{2}^-$	$(0.01, 108^\circ)$ $(0.01, 117^\circ)$	$(0.25, 82^\circ)$ $(0.30, 89^\circ)$	$(0.00, -51^\circ)$ $(0.00, -48^\circ)$
$N(1680)\frac{5}{2}^+$	$(0.00, -8^\circ)$ $(0.00, -32^\circ)$	$(0.04, 31^\circ)$ $(0.04, 26^\circ)$	$(0.95, 165^\circ)$ $(0.98, 162^\circ)$
$N(1990)\frac{7}{2}^+$	$(0.00, -46^\circ)$ $(0.00, -42^\circ)$	$(0.04, -60^\circ)$ $(0.04, -62^\circ)$	$(0.00, -105^\circ)$ $(0.00, -107^\circ)$
$N(2190)\frac{7}{2}^-$	$(0.00, -155^\circ)$ $(0.00, -149^\circ)$	$(0.01, 146^\circ)$ $(0.01, 154^\circ)$	$(0.07, 177^\circ)$ $(0.03, 177^\circ)$
$N(2250)\frac{9}{2}^-$	$(0.01, -31^\circ)$ $(0.01, -47^\circ)$	$(0.12, -28^\circ)$ $(0.16, -38^\circ)$	$(0.00, -42^\circ)$ $(0.01, -52^\circ)$
2nd pole $\frac{9}{2}^-$	$(0.00, 92^\circ)$ $(0.00, 83^\circ)$	$(0.06, 85^\circ)$ $(0.05, 78^\circ)$	$(0.00, 44^\circ)$ $(0.00, 44^\circ)$
$N(2220)\frac{9}{2}^+$	$(0.00, 50^\circ)$ $(0.00, 58^\circ)$	$(0.01, 10^\circ)$ $(0.01, 14^\circ)$	$(0.03, 21^\circ)$ $(0.03, 24^\circ)$